Fourth Semester B.E. Degree Examination, June/July 2017 Engineering Mathematics-IV

Time: 3 hrs.
Max. Marks: 80

## Note: 1. Answer FIVE full questions, choosing one full question from each module. 2. Use of statistical tables are permitted.

## Module-1

1 a. Find by Taylor's series method the value of $y$ at $x=0.1$ from $\frac{d y}{d x}=x^{2} y-1, y(0)=1$ (upto $4^{\text {th }}$ degree term).
(05 Marks)
b. The following table gives the solution of $5 x^{\prime}+y^{2}-2=0$. Find the value of $y$ at $x=4.5$ using Milne's predictor and corrector formulae.
(05 Marks)

| x | 4 | 4.1 | 4.2 | 4.3 | 4.4 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| y | 1 | 1.0049 | 1.0097 | 1.0143 | 1.0187 |

c. Using Euler's modified method. Obtain a solution of the equation $\frac{d y}{d x}=x+|\sqrt{y}|$, with initial conditions $y=1$ at $x=0$, for the range $0 \leq x \leq 0.4$ in steps of 0.2 .
(06 Marks)

## OR

2 a. Using modified Euler's method find $y(20.2)$ and $y(20.4)$ given that $\frac{d y}{d x}=\log _{10}\left(\frac{x}{y}\right)$ with $y(20)=5$ taking $\mathrm{h}=0.2$.
(05 Marks)
b. Given $\frac{d y}{d x}=x^{2}(1+y)$ and $y(1)=1, y(1.1)=1.233, y(1.2)=1.548, y(1.3)=1.979$. Evaluate $y(1.4)$ by Adams-Bashforth method.
(05 Marks)
c. Using Runge-Kutta method of fourth order, solve $\frac{d y}{d x}=\frac{y^{2}-x^{2}}{y^{2}+x^{2}}$ with $y(0)=1$ at $x=0.2$ by taking $\mathrm{h}=0.2$
(06 Marks)

## Module-2

3 a. Obtain the solution of the equation $2 \frac{d^{2} y}{d x^{2}}=u x+\frac{d y}{d x}$ by computing the value of the dependent variable corresponding to the value 1.4 of the independent variable by applying Milne's method using the following data:
(05 Marks)

| x | 1 | 1.1 | 1.2 | 1.3 |
| :---: | :---: | :---: | :---: | :---: |
| y | 2 | 2.2156 | 2.4649 | 2.7514 |
| $\mathrm{y}^{\prime}$ | 2 | 2.3178 | 2.6725 | 3.0657 |

b. Express $f(x)=3 x^{3}-x^{2}+5 x-2$ in terms of Legendre polynomials.
(05 Marks)
c. Obtain the series solution of Bessel's differential equation $x^{2} y^{\prime \prime}+x y^{\prime}+\left(x^{2}+n^{2}\right) y=0$
(06 Marks)

## OR

4 a. By Runge-Kutta method solve $\frac{d^{2} y}{d x^{2}}=x\left(\frac{d y}{d x}\right)^{2}-y^{2}$ for $x=0.2$. Correct to four decimal places using the initial conditions $\mathrm{y}=1$ and $\mathrm{y}^{\prime}=0$ at $\mathrm{x}=0, \mathrm{~h}=0.2$.
(05 Marks)
b. Prove that $\mathrm{J}_{+\frac{1}{2}}(\mathrm{x})=\sqrt{\frac{2}{\pi \mathrm{x}}} \sin \mathrm{x}$
(05 Marks)
c. Prove the Rodrigues formula,

$$
\rho_{n}(x)=\frac{1}{2^{n} n!} \frac{d^{n}\left(x^{2}-1\right)^{n}}{d x^{n}}
$$

(06 Marks)

## Module-3

5 a. State and prove Cauchy's-Riemann equation in polar form.
(05 Marks)
b. Discuss the transformation $\mathrm{W}=\mathrm{e}^{\mathrm{z}}$.
(05 Marks)
c. Evaluate $\int_{C}\left\{\frac{\sin \left(\pi z^{2}\right)+\cos \left(\pi z^{2}\right)}{(z-1)^{2}(z-2)}\right\} d z$
using Cauchy's residue theorem where ' $C$ ' is the circle $|z|=3$
(06 Marks)

## OR

6 a. Find the analytic function whose real part is, $\frac{\sin 2 x}{\cosh 2 y-\cos 2 x}$.
(05 Marks)
b. State and prove Cauchy's integral formula.
(05 Marks)
c. Find the bilinear transformation which maps $z=\infty, i, 0$ into $\omega=-1,-i, 1$. Also find the fixed points of the transformation.
(06 Marks)

## Module-4

7 a. Find the mean and standard deviation of Poisson distribution.
(05 Marks)
b. In a test on 2000 electric bulbs, it was found that the life of a particular make was normally distributed with an average life of 2040 hours and S.D of 60 hours. Estimate the number of bulbs likely to burn for,
(i) more than 2150 hours.
(ii) less than 1950 hours
(iii) more than 1920 hours and less than 2160 hours.
$[\mathrm{A}(1.833)=0.4664, \mathrm{~A}(1.5)=0.4332, \mathrm{~A}(2)=0.4772]$
(05 Marks)
c. The joint probability distribution of two random variables x and y is as follows:

| $\mathrm{x} / \mathrm{y}$ | -4 | 2 | 7 |
| :---: | :---: | :---: | :---: |
| 1 | $1 / 8$ | $1 / 4$ | $1 / 8$ |
| 5 | $1 / 4$ | $1 / 8$ | $1 / 8$ |

Determine:
(i) Marginal distribution of $x$ and $y$.
(ii) Covariance of x and y
(iii) Correlaiton of $x$ and $y$.

## OR

8 a. The probability that a pen manufactured by a factory be defective is $\frac{1}{10}$. If 12 such pens are manufactured what is the probability that, (i) Exactly 2 are defective (ii) at least 2 are defective (iii) none of them are defective.
b. Derive the expressions for mean and variance of binomial distribution.
c. A random variable X take the values $-3,-2,-1,0,1,2,3$ such that $\mathrm{P}(\mathrm{x}=0)=\mathrm{P}(\mathrm{x}<0)$ and $P(x=-3)=P(x=-2)=P(x=-1)=P(x=1)=P(x=2)=P(x=3)$. Find the probability distribution.
(06 Marks)

## Module-5

9 a. In 324 throws of a six faced 'die' an odd number turned up 181 times. Is it reasonable to think that the 'die' is an unbiased one?
(05 Marks)
b. Two horses A and B were tested according to the time (in seconds) to run a particular race with the following results:

| Horse A: | 28 | 30 | 32 | 33 | 33 | 29 | 34 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Horse B: | 29 | 30 | 30 | 24 | 27 | 29 |  |

Test whether you can discriminate between the two horses. $\left(\mathrm{t}_{0.05}=2.2\right.$ and $\mathrm{t}_{0.02}=2.72$ for 11 d.f) ( 05 Marks)
c. Find the unique fixed probability vector for the regular stochastic matrix, $A=\left[\begin{array}{ccc}0 & 1 & 0 \\ 1 / 6 & 1 / 2 & 1 / 3 \\ 0 & 2 / 3 & 1 / 3\end{array}\right]$
(06 Marks)

## OR

a. Define the terms: (i) Null hypothesis (ii) Type-I and Type-II error (iii) Confidence limits.
(05 Marks)
b. Prove that the Markov chain whose t.p.m $P=\left[\begin{array}{ccc}0 & 2 / 3 & 1 / 3 \\ 1 / 2 & 0 & 1 / 2 \\ 1 / 2 & 1 / 2 & 0\end{array}\right]$ is irreducible. Find the corresponding stationary probability vector.
(05 Marks)
c. Three boys $\mathrm{A}, \mathrm{B}, \mathrm{C}$ are throwing ball to each other. A always throws the ball to B and B always throws the ball to $\mathrm{C} . \mathrm{C}$ is just as likely to throw the ball to B as to A . If C was the first person to throw the ball find the probabilities that after three throws (i) A has the ball.
(ii) B has the ball. (iii) C has the ball.
(06 Marks)


15EC42

Fourth Semester B.E. Degree Examination, June/July 2017 Microprocessor

Time: 3 hrs .
Max. Marks: 80

## Note: Answer FIVE full questions, choosing one full question from each module.

## Module-1

1 a. Explain the internal architecture of 8086 with its neat block diagram.
(08 Marks)
b. Explain briefly any 4 addressing modes of data of 8086 with an example for each. ( 06 Marks)
c. If CS $=1000 \mathrm{H}, \mathrm{DS}=25 \mathrm{~A} 0 \mathrm{H}, \mathrm{SS}=3210 \mathrm{H}, \mathrm{ES}=5890 \mathrm{H}, \mathrm{BX}=43 \mathrm{~A} 9 \mathrm{H}, \mathrm{BP}=3400 \mathrm{H}$, find the physical address of the source data for the following instructions:
(i) MOV AL, $[\mathrm{BX}+1200 \mathrm{H}]$
(ii) $\mathrm{ADD} \mathrm{BL},[\mathrm{BP}+05]$
(02 Marks)
OR
2 a. Write down the instruction formats for the following two types of cases of 8086 and form theopode for the indicated instruction:
(i) Register to Register; ADD AX, BX
(ii) Immediate to Register; ADD CX, 1200 H .
(06 Marks)
b. Write 8086 program to find the smallest number out of N 16 bit unsigned numbers stored in a memory block starting with the address 2000 H. Store the result at word location 3000 H .
(08 Marks)
c. Briefly explain the following 8086 instructions:
(i) XLAT
(ii)
NEG
(02 Marks)

## Module- 2

3 a. Write a complete assembly language program in 8086 which replaces all the occurances of character '-' in a given string by '*'.
(08 Marks)
b. Verify whether any of the following instructions are wrong and correct them with reasons. Assuming following is a program, what is the value of register BX and flags $\mathrm{CY}, \mathrm{Z}, \mathrm{P}, \mathrm{S}$ at the end.

| (i) | MOV BX, 0804H |
| :--- | :--- |
| (ii) | INC [BX +02$]$ |
| (iii) | ADD 06H, AL |
| (iv) | SHR DX, 02 |
| (v) | XOR BL, BL |

(08 Marks)
OR .
4 a. Briefly explain the operations of the string instructions of 8086 , indicating the initializations required to use them.
(06 Marks)
b. Write a complete assembly language program for block move of a source data (10 bytes) present in a memory block starting with address SOURCE to a destination block starting from address DSTN, using MOVS instruction. Consider overlapping of blocks also.
c. Explain briefly any 4 assembler directives.
(02 Marks)

## Module-3

5 a. (i) Explain the stack structure of 8086 and the operations of PUSH and POP instructions.
(ii) Sketch the content of stack memory indicating the value of SP register before PUSH BX operation and after the PUSH BX operation. Assume $\mathrm{SS}=2500 \mathrm{H}, \mathrm{BX}=432 \mathrm{AH}$ and $\mathrm{SP}=1000 \mathrm{H}$.
(08 Marks)
b. Write a procedure in 8086 assembly language which computes the factorial of an 8 bit number passed through AL register. The factorial value (maximum 8 bit) is returned through AL register.
(08 Marks)
a. What are the sequence of actions taken by 8086 and the device, when a device interrupts 8086 over INTR line? Explain about the software and reserved internal interrupts of 8086 .
(08 Marks)
b. What are the differences between a procedure and a macro? Create a macro that would find the logical NAND value of two operands.
(04 Marks)
c. What are the methods that can be used to pass parameters to a procedure? Explain any one of them with an example.
(04 Marks)

## Module-4

7 a. Sketch the minimum mode configuration of 8086 and explain the operation briefly.
(08 Marks)
b. Interface two $4 \mathrm{~K} \times 8 \mathrm{EPROM}$ and two $4 \mathrm{~K} \times 8$ static RAM chips to 8086 . The addresses of RAM and ROM should start from FC 000 H and FE 000 H respectively.
(08 Marks)

## OR

a. Sketch the maximum mode configuration of 8086 and explain the operation briefly.
(08 Marks)
b. Interface a 7 -segment LED to 8086 using a 74 LS 373 latch for I/O address 0 CH . Write a program that simulates a single digit seconds counter on the LED digit. (Assume a one second software delay is available)
(08 Marks)

## Module-5

9 a. Interface $\mathrm{ADC} 0808 / 0809$ to 8086 using 8255 and write a program to convert the analog voltage connected to the last channel. Store the digital value in the location 2000 H .
(08 Marks)
b. Interface a stepper motor to 8086 using 8255 and write a program to rotate the motor in clockwise direction 5 steps or in counter clockwise direction 10 steps, depending on whether the content of memory location 2000 H is 00 H or FFH respectively.
(08 Marks)

## OR

10 a. Explain the architecture of NDP-8087 with its internal block diagram.
(08 Marks)
b. Write a program in 8086 using DOS 21 H interrupt which waits for a key to be pressed from the keyboard. If the key is ' $G$ ' display the message 'GOOD' on the CRT and display the message 'VERY GOOD', if the key V is pressed. Display 'NOT VALID' if any other key is pressed.
(05 Marks)
c. Explain mode-2 operation of 8254 timer briefly. What is the control word to be used to operate counter-1 in mode-2 binary?
(03 Marks)

## CBCS Scheme <br> USN <br> $\square$ <br> Fourth Semester B.E. Degree Examination, June/July 2017 Control Systems

Time: 3 hrs.
Max. Marks: 80
Note: Answer FIVE full questions, choosing one full question from each module.

## Module-1

1 a. Explain linear and non-linear control system.
(04 Marks)
b. For the mechanical system shown in Fig.Q1(b):
i) Draw the mechanical network.
ii) Obtain equations of motion.
iii) Draw an electrical network based on force current analogy.
(06 Marks)


Fig.Q1(b)


Fig.Q1(c)
c. For the signal flow graph shown in Fig.Q1(c), determine the transfer function $\frac{C(s)}{R(s)}$ using Mason's gain formula
(06 Marks)

## OR

2 a. For the circuit shown in Fig.Q2(a), ' K ' is the gain of an ideal amplifier. Determine the transfer function $\frac{\mathrm{I}(\mathrm{s})}{\mathrm{V}_{\mathrm{i}}(\mathrm{s})}$.


Fig.Q2(a)
b. For the mechanical system shown in Fig.Q2(b):
i) Draw equivalent mechanical network.
ii) Write performance equations.
iii) Draw torque-voltage analogy.


Fig.Q2(b)
(06 Marks)
c. Obtain $\frac{C(s)}{R(s)}$ for the block diagram shown in Fig.Q2(c) using block diagram reduction techniques.


Fig.Q2(c)
(06 Marks)

## Module -2

3 a. List the standard test inputs used in control system and write their Laplace transform.
(04 Marks)
b. Find $K_{p}, K_{v}, K_{a}$ and steady state error for a system with open loop transfer function as

$$
\mathrm{G}(\mathrm{~s}) \mathrm{H}(\mathrm{~s})=\frac{10(\mathrm{~s}+2)(\mathrm{s}+3)}{\mathrm{s}(\mathrm{~s}+1)(\mathrm{s}+4)(\mathrm{s}+5)}
$$

where the input is $r(t)=3+t+t^{2}$.
(06 Marks)
c. For the system shown in Fig.Q3(c), obtain closed loop transfer function, damping ratio natural frequency and expression for the output response if subjected to unit step input.

(06 Marks)

## OR

4 a. Define rise time and maximum overshoot and write their formula.
(04 Marks)
b. For a given system $G(s) H(s)=\frac{K}{s^{2}(s+2)(s+3)}$. Find the value of $K$ to limit steady state error to 10 when input to system is $1+10 t+20 t^{2}$.
(06 Marks)
c. For a unity feedback control system with $G(s)=\frac{64}{s(s+9.6)}$. Write the output response to a unit step input. Determine:
i) The response at $t=0.1 \mathrm{sec}$.
ii) Settling time for $\pm 2 \%$ of steady state.
(06 Marks)

## Module-3

5 a. Explain Rouths-Harwitz stability criterion.
(04 Marks)
b. $s^{6}+4 s^{5}+3 s^{4}-16 s^{2}-64 s-48=0$. Find the number of roots of this equation with positive real part, zero real part and negative real part using RH criterion.
(06 Marks)
c. Sketch the rough nature of the root locus of a certain control system whose characteristic equation is given by $s^{3}+9 s^{2}+K s+K=0$, comment on the stability.
(06 Marks)

6 a. The open loop transfer function of a unity feedback system is $G(s)=\frac{K(s+2)}{s(s+3)\left(s^{2}+5 s+10\right)}$.
i) Find the value of $K$ so that the steady state error for the input $r(t)=t u(t)$ is less than or equal to 0.01 .
ii) For the value of K found in part (i). Verify whether the closed loop system is stable or not using R-H criterion.
(06 Marks)
b. Sketch the root locus plot for a negative feedback control system whose open loop transfer function is given by $\mathrm{G}(\mathrm{s}) \mathrm{H}(\mathrm{s})=\frac{\mathrm{K}}{\mathrm{s}(\mathrm{s}+3)\left(\mathrm{s}^{2}+2 \mathrm{~s}+2\right)}$ for all values of K ranging from 0 to $\infty$. Also find the value of K for a damping ratio of 0.5 .
(10 Marks)

## Module-4

7 a. For a closed loop control system $\mathrm{G}(\mathrm{s})=\frac{100}{\mathrm{~s}(\mathrm{~s}+8)}, \mathrm{H}(\mathrm{s})=1$. Determine the resonant peak and resonant frequency.
(04 Marks)
b. Explain lag-lead compensator network and briefly discuss the effects of lead-lag compensator.
(04 Marks)
c. Using Nyquist stability criterion, find the closed loop stability of a negative feedback control system whose open-loop transfer function is given by $G(s) H(s)=\frac{5}{s(s-1)}$.
(08 Marks)

## OR

8 a. Draw polar plot of $G(s) H(s)=\frac{100}{s^{2}+10 s+100}$.
(06 Marks)
b. For a unity feedback system $G(s)=\frac{242(s+5)}{s(s+1)\left(s^{2}+5 s+121\right)}$. Sketch the bode plot and find $\omega_{\mathrm{gc}}, \omega_{\mathrm{pc}}$, gain margin and phase margin.
(10 Marks)

## Module-5

9 a. With block diagram, explain system with digital controller.
(04 Marks)
b. Obtain the state model for the system represented by the differential equation $\frac{d^{3} y(t)}{d t^{3}}+6 \frac{d^{2} y(t)}{d t^{2}}+11 \frac{d y(t)}{d t}+10 y(t)=3 u(t)$.
(04 Marks)
c. Find the transfer function of the system having state model.

$$
\begin{array}{r}
\dot{X}=\left[\begin{array}{cc}
0 & 1 \\
-2 & -3
\end{array}\right]\left[\begin{array}{l}
x_{1} \\
x_{2}
\end{array}\right]+\left[\begin{array}{l}
0 \\
1
\end{array}\right] u \text { and } y=\left[\begin{array}{ll}
1 & 0
\end{array}\right]\left[\begin{array}{l}
x_{1} \\
x_{2}
\end{array}\right] \\
\text { OR }
\end{array}
$$

10 a. Explain signal reconstruction scheme using sampler and zero order hold.
(04 Marks)
b. Obtain the state model of given electrical network shown in Fig.Q10(b).


Fig.Q10(b)
(04 Marks)
c. Find the state transition matrix for $\mathrm{A}=\left[\begin{array}{ll}0 & -1 \\ 2 & -3\end{array}\right]$.
(08 Marks)

## CBCS Scheme

USN


15EC44

Fourth Semester B.E. Degree Examination, June/July 2017
Signals and Systems

Time: 3 hrs .
Max. Marks: 80
Note: Answer any FIVE full questions, choosing one full question from each module.

## Module-1

1 a. Sketch the even and odd part of the signals shown in Fig. Q1 (a) and (b).
(08 Marks)


Fig. Q1(a)


Fig. Q1(b)
b. Determine whether the following signal is periodic or not if periodic find the fundamental period. $x(n)=\cos \left(\frac{n \pi}{5}\right) \sin \left(\frac{n \pi}{3}\right)$
(03 Marks)
c. Express $x(t)$ in terms $g(t)$ if $x(t)$ and $g(t)$ are shown in Fig. Q1 (c).
(05 Marks)


Fig. Q1(c)
OR
2 a. Determine whether the following systems are memory less, causal, time invariant, linear and stable. i) $y(n)=n x(n) \quad$ ii) $y(t)=x(t / 2)$.
(08 Marks)
b. For the signal $x(t)$ and $y(t)$ shown in Fig. Q2(b) sketch the following signals.
i) $x(t+1) \cdot y(t-2)$
ii) $x(t) \cdot y(t-1)$
(08 Marks)


Fig. Q2(b)

## Module-2

3 a. Prove the following:
i) $\mathrm{x}(\mathrm{n}) *\left[\mathrm{~h}_{1}(\mathrm{n})+\mathrm{h}_{2}(\mathrm{n})\right]=\mathrm{x}(\mathrm{n}) * \mathrm{~h}_{1}(\mathrm{n})+\mathrm{x}(\mathrm{n}) * \mathrm{~h}_{2}(\mathrm{n})$
ii) $\mathrm{x}(\mathrm{n}) * \mathrm{u}(\mathrm{n})=\sum_{\mathrm{k}=-\infty}^{\mathrm{n}} \mathrm{x}(\mathrm{k})$.
(08 Marks)
b. Compute the convolution sum of $x(n)=u(n)-u(n-8)$ and $h(n)=u(n)-u(n-5)$. (08 Marks)

## OR

4 a. State and prove the associative, integral and commutative properties of convolution.
(08 Marks)
b. Compute the convolution integral of $x(t)=u(t)-u(t-2)$ and $h(t)=e^{-t} u(t)$.
(08 Marks)

## Module-3

5 a. A system consists of several subsystems connected as shown in Fig. Q5(a). Find the operator H relating $x(t)$ to $y(t)$ for the following sub system operators.
(04 Marks)


Fig. Q5(a)
b. Determine whether the following systems defined by their impulse responses are causal, memory less and stable.
i) $h(t)=e^{-2 t} u(t-1) \quad$ ii) $h(n)=2 u[n]-2 u(n-5)$
(06 Marks)
c. Evaluate the step response for the LTI systems represented by the following impulse responses. i) $h(t)=u(t+1)-u(t-1)$
ii) $\mathrm{h}(\mathrm{n})=\left(\frac{1}{2}\right)^{\mathrm{n}} \mathrm{u}(\mathrm{n})$.
(06 Marks)

## OR

a. State the following properties of CTFS. i) Time shift ii) Differentiation in time domain iii) Linearity
iv) Convolution
v) Frequency shift
vi) Scaling.
(06 Marks)
b. Determine the DTFS coefficients for the signal shown in Fig.Q6 (b) and also plot $|\mathrm{x}(\mathrm{k})|$ and $\arg \{\mathrm{x}(\mathrm{k})\}$.
(10 Marks)


Fig. Q6(b)

## Module-4

7 a. State and prove the following properties:
i) $y(t)=h(t) * x(t) \stackrel{F T}{\longleftrightarrow} y(j w)=x(j w) H(j w)$
ii) $\frac{\mathrm{d}}{\mathrm{dt}} \mathrm{x}(\mathrm{t}) \stackrel{\mathrm{FT}}{\longleftrightarrow} \mathrm{jw} \mathrm{x}(\mathrm{jw})$
(06 Marks)
b. Find DTFT of the following signals.
i) $\mathrm{x}(\mathrm{n})=\{1,2,3,2,1\}$
ii) $x(n)=\left(\frac{3}{4}\right)^{n} u[n]$.
(10 Marks)

## OR

8 a. Specify the Nyquist rate for the following signals
i) $x_{1}(t)=\sin (200 \pi t)$
ii) $x_{2}(t)=\sin (200 \pi t)+\cos (400 \pi t)$.
(04 Marks)
b. Use partial fraction expansion to determine the time domain signals corresponding to the following FTs.
i) $x(j w)=\frac{-j w}{(j w)^{2}+3 j w+2}$
ii) $x(j w)=\frac{j w}{(j w+2)^{2}}$
(08 Marks)
c. Find FT of the signal $x(t)=e^{-2 t} u(t-3)$.
(04 Marks)

## Module-5

9 a. Explain properties of ROC with example.
(06 Marks)
b. Determine the z-transform of the following signals

$$
\begin{aligned}
& \text { i) } \quad x(n)=\left(\frac{1}{4}\right)^{n} u(n)-\left(\frac{1}{2}\right)^{n} u(-n-1) \\
& \text { ii) } \quad x(n)=n\left(\frac{1}{2}\right)^{n} u(n)
\end{aligned}
$$

(10 Marks)

10 a. Find the time domain signals corresponding to the following z-transforms.

$$
\begin{equation*}
x(z)=\frac{\left(\frac{1}{4}\right) z^{-1}}{\left(1-\frac{1}{2} z^{-1}\right)\left(1-\frac{1}{4} z^{-1}\right)} \text { with ROC } \frac{1}{4}<|z|<\frac{1}{2} \tag{06Marks}
\end{equation*}
$$

b. Determine the transfer function and the impulse response for the causal LTI system described by the difference equation

$$
y(n)-\frac{1}{4} y(n-1)-\frac{3}{8} y(n-2)=-x(n)+2 x(n-1)
$$



15 EC 45

Fourth Semester B.E. Degree Examination, June/July 2017
Principles of Communication Systems
Time: 3 hrs.
Max. Marks: 80
Note: Answer FIVE full questions, choosing one full question from each module.

## Module-1

1 a. Explain with the help of a neat sketch and analysis, how switching modulator is used to generate amplitude modulation.
(06 Marks)
b. Explain how Costas receiver can be used for demodulating the DSB-SC signal. ( $\mathbf{0 6}$ Marks)
c. Consider a message signal $\mathrm{m}(\mathrm{t})$ containing frequency components at 100,200 and 400 Hz . This signal is applied to an SSB modulator together with a carrier at 100 kHz , with only the upper sideband retained. In the coherent detector used to recover $m(t)$, the local oscillator supplies a sine wave of frequency 100.02 kHz .
i) Determine the frequency components of the detector output.
ii) Repeat the analysis assuming that only the lower sideband is transmitted. ( 04 Marks)

## OR

2 a. Explain the operation of envelope detector with neat diagrams and waveforms. Bring out the significance of the RC time constant of the circuit in detection of the message signal without distortion.
(06 Marks)
b. Derive an expression for SSB modulated wave for which upper side band is retained.
(06 Marks)
c. Using the message signal $\mathrm{m}(\mathrm{t})=\frac{1}{1+\mathrm{t}^{2}}$, determine and sketch the modulated wave for amplitude modulation with the following values. (i) $\mu=50 \%$, (ii) $100 \%$.
(04 Marks)

## Module-2

3 a. Derive the equation for frequency modulated wave. Define modulation index, maximum deviation of a frequency modulated signal.
(06 Marks)
b. Explain generation of frequency modulated signal using direct method.
(05 Marks)
c. The equation for a $F M$ wave is $s(t)=10 \sin \left[5.7 \times 10^{8} t+5 \sin 12 \times 10^{3} t\right]$. Calculate :
i) Carrier frequency
ii) Modulating frequency
iii) Modulation index
iv) Frequency deviation
v) Power dissipated in $100 \Omega$
(05 Marks)

## OR

4 a. With neat circuit diagram, explain FM demodulation using balanced slope detector.
b. With relevant block diagram, explain FM stereo multiplexing. (06 Marks)
c. Explain the linear model of phase locked loop (PLL). (05 Marks)

## Module-3

5 a. What is conditional probability? Prove that $P(B / A)=\frac{P(A / B) \cdot P(B)}{P(A)}$.
(05 Marks)
b. With an example, explain what is meant by statistical averages.
(06 Marks)
c. Define white noise. Plot power spectral density (PSD) and autocorrelation function (ACF) of white noise.
(05 Marks)

## OR

6 a. What do you mean by probability density function? Prove that the total volume under the surface of a probability density function (pdf) is always 1 .
(05 Marks)
b. Define mean, autocorrelation and auto-covariance function.
(06 Marks)
c. What is noise equivalent band width? Derive an expression for the same.
(05 Marks)

## Module-4

7 a. With relevant equations, explain how noise is produced in a receiver model.
(08 Marks)
b. Show that the figure-of-merit for DSB-SC system is unity.
(08 Marks)

## OR

8 a. Derive the expression for figure-of-merit of an AM receiver.
(08 Marks)
b. Explain pre-emphasis and de-emphasis in frequency modulation (FM).
(08 Marks)

## Module-5

9 a. State sampling theorem for band limited signals. Explain the process of sampling. ( 07 Marks)
b. With neat block diagram, explain the generation of pulse-position modulation (PPM) waves.
(05 Marks)
c. Twelve different message signals, each with a bandwidth of 10 kHz are to be multiplexed and transmitted. Determine the minimum bandwidth required for each method if the multiplexing/modulation method used is (i) FDM, SSB; (ii) TDM, PAM.
(04 Marks)

## OR

10 a. With relevant diagram, explain the generation and reconstruction of pulse code modulation (PCM) signal.
(06 Marks)
b. With neat diagram, explain the concept of time division multiplexing (TDM).
c. Determine the Nyquist rate and the Nyquist interval for:
(i) $\mathrm{g}(\mathrm{t})=\sin \mathrm{c}(200 \mathrm{t})$
(ii) $\mathrm{m}(\mathrm{t})=\frac{1}{\pi \mathrm{t}}[\sin (500 \pi \mathrm{t})]$.
(04 Marks)

# GBCS Scheme <br>  <br> Fourth Semester B.E. Degree Examination, June/July 2017 Linear Integrated Circuits 

15EC46

Time: 3 hrs .
Max. Marks: 80
Note: Answer FIVE full questions, choosing one full question from each module.

## Module- 1

1 a. With a neat circuit diagram, explain basic operational amplifier circuit.
(06 Marks)
b. Define CMRR of an operational amplifier. A741 op-amp is used in a non-inverting amplifier with a voltage gain of 50 . Calculate the typical output voltage that would result from a common mode input with a peak level of 100 mV .
(05 Marks)
c. Design an averaging circuit to give the average of two inputs which each range from 0.1 V to 1 V . Use 741 op-amp.
(05 Marks)

## OR

2 a. Sketch the circuit of an op-amp difference amplifier circuit. Discuss the working and common mode nulling capability with necessary circuit modification and equations.
(08 Marks)
b. With a neat circuit diagram, explain direct coupled voltage follower. Also compare voltage follower with emitter follower.
(08 Marks)

## Module-2

3 a. Draw the circuit of a capacitor coupled non-inverting amplifier and explain with necessary design equations. Design a high input impedance capacitor coupled non-inverting amplifier with a gain of 100 and lower cut off frequency of 100 Hz . Assume the load resistance is $2.2 \mathrm{~K} \Omega$ and input parasitic capacitance as 15 pF .
(10 Marks)
b. Design a capacitor coupled inverting amplifier for a pass band gain of 100 , lower cut off frequency of 120 Hz and upper cutoff frequency to be 5 kHz . Use LF353 BIFET opamp and assume load resistance as $2 \mathrm{~K} \Omega$.
(06 Marks)

## OR

4 a. Draw the circuit of an instrumentation amplifier and explain. Also show the method of nulling common mode outputs and how dc output voltage can be level shifted.
(09 Marks)
b. Design a non-saturating precision half wave rectifier to produce a 2 V peak output from a 1 MHz sine waye input with a 0.5 V peak value. Use a bipolar op-amp with a supply voltage of $\pm 15 \mathrm{~V}$.
(07 Marks)

## Module-3

5 a. Sketch the circuit of a symmetrical precision clipper and explain with necessary equations and waveforms. Using bipolar opamp design the circuit to clip a 100 kHz sine wave at $\pm 3 \mathrm{~V}$ level.
(09 Marks)
b. Explain the working of Weinbridge oscillator with the help of circuit diagram, waveforms and equations.
(07 Marks)

## OR

6 a. Sketch the circuit of fundamental log amplifier and explain its operation. Also derive an expression for its output voltage. Also mention its drawback.
(08 Marks)
b. With a neat circuit diagram, explain the operation of inverting Schmitt trigger. Using 741 op-amp with a supply of $\pm 12 \mathrm{~V}$, design an inverting Schmitt trigger circuit to have trigger points of UTP $=0 \mathrm{~V}$ and LTP $=-1 \mathrm{~V}$.
(08 Marks)

## Module-4

7 a. Explain the operation of first order low pass filter with neat circuit diagram, frequency response and design steps. Using a 741 opamp, design a first order active low pass filter to have a cutoff frequency of 2 kHz .
(08 Marks)
b. Draw the circuit of a single stage band pass filter and explain the operation with necessary design equations.
(08 Marks)

## OR

8 a. Draw the standard representation of 78XX series 3-terminal IC regulator and enumerate the characteristics of this type of regulators. Also define the following performance parameters of a voltage regulator. (i) Line regulation (ii) Load regulation (iii) Ripple rejection
(08 Marks)
b. With a neat diagram, explain the operation of low voltage regulator using IC723. Design a voltage regulator circuit using LM723 to obtain $\mathrm{V}_{0}=5 \mathrm{~V}$ and $\mathrm{I}_{0}=2 \mathrm{~A}$.
(08 Marks)

## Module-5

9 a. With a neat block schematic, explain the operating principle of PLL. Also define (i) Lock-in range (ii) Capture range and (iii) Pull-in time.
(08 Marks)
b. Explain the working of Flash ADC with necessary diagram. An 8 bit ADC outputs all 1's when $V_{i}=2.55 \mathrm{~V}$. Find its (i) resolution in mV/LSB and (ii) digital output when $\mathrm{V}_{\mathrm{i}}=1.28 \mathrm{~V}$
(08 Marks)

## OR

10 a. Draw the internal schematic of IC555, configuring it for astable operation and explain with necessary equations and waveforms.
(08 Marks)
b. With necessary circuit diagram and equations, explain R-2R DAC. What output voltage would be produced by a DAC whose output range is 0 to 10 V and whose input binary number is, (i) 1010 (for 4 bit DAC) (ii) 10111100 (for an 8 bit DAC).
(08 Marks)


15EI/BM/ML42

## Fourth Semester B.E. Degree Examination, June/July 2017 <br> Signal Conditioning and Data Acquisition Circuits

Time: 3 hrs .
Max. Marks: 80
Note: Answer any FIVE full questions, choosing one full question from each module.

## Module- 1

1 a. With the help of circuit schematic mention how we can obtain symmetrical supply voltage by using fixed power supply and zener diodes.
(03 Marks)
b. Calculate the total current $i_{0}$ following into the output pin of an inverting amplifier with $\mathrm{v}_{\mathrm{i}}=1 \mathrm{v}$, feedback resistance of $100 \mathrm{k} \Omega$, load resistance of $25 \mathrm{k} \Omega$ and a closed loop voltage gain of -10 .
(05 Marks)
c. Draw the equivalent circuit of a practical opamp inverting amplifier and derive the expression for closed loop voltage gain.
(08 Marks)

## OR

2 a. Derive the expression for output voltage of a Non-inverting summing amplifier. (07 Marks)
b. A non inverting amplifier with a gain of 100 is nulled at $25^{\circ} \mathrm{C}$. What will happen to the output voltage if the temperature rises to $50^{\circ} \mathrm{C}$ for an offset voltage drift of $0.15 \mathrm{mV} /{ }^{\circ} \mathrm{C}$.?
(02 Marks)
c. Mention the salient features of instrumentation amplifier. Explain how instrumentation amplifier can be employed in the signal conditioning circuit for transducer bridge. (07 Marks)

## Module- 2

3 a. Draw the circuit schematic of V to I converter with grounded load and derive the expression for output current.
(05 Marks)
b. With the help of circuit diagram explain the operating principle of precision full wave
(06 Marks)
c. Design a practical differentiator using opamp that will differentiate an input signal with $f_{a}=f_{\text {max }}=100 \mathrm{~Hz}, \mathrm{f}_{\mathrm{b}}=1 \mathrm{KHz}$ and $\mathrm{c}_{1}=0.1 \mu \mathrm{~F}$.
(05 Marks)

## OR

4 a. With circuit diagram explain how comparator can be used to construct three level window detector and time marker generator.
(08 Marks)
b. Draw the circuit schematic of opamp based astabe multi-vibrator and explain its working principle.
(08 Marks)

## Module-3

5 a. Define the terms line regulation and load regulation with respect to voltage regulator.

$$
1
$$

(02 Marks)
b. Draw the functional block diagram of low voltage regulator and explain.
(08 Marks)
c. Specify the limitations of linear voltage regulator. Explain how these limitations can be overcome by using switching regulator.
(06 Marks)

## OR

6 a. Design a second order low pass filter with highicutoff frequency of 1 KHz if the capacitances of $0.0047 \mu \mathrm{~F}$ are to be used.
(05 Marks)
b. Write the circuit schematic of Narrow Band-pass Filter and write the design procedure.
(07 Marks)
c. Write the circuit schematic of Narrow Band Reject Filter and design a 50 Hz active notch filter.
(04 Marks)

## Module-4

7 a. Draw the functional diagram of IC 555 timer and explain.
(06 Marks)
b. With the help of circuit schematic explain the working principle of mono-stable multivibrator using IC 555 timer.
(05 Marks)
c. Draw the circuit of FSIK generator using IC 555 . Explain how FSK signal can be generated by configuring IC 555 timer in astable mode.
(05 Marks)

OR
8 a. Define the terms capture range and Lock-in range with respect to PLL.
(04 Marks)
b. Give the block diagram of IC 566 VCO and explain its principle of operation.
(07 Marks)
c. With the help of block diagram explain how PLL can be used as frequency translator.
(05 Marks)

## Module-5

9 a. Draw the generalized diagram of digital data acquisition system and explain the function of its constituent blocks.
(09 Marks)
b. Mention the basis on which we select analog/digital data acquisition system for a particular application.
c. Discuss about the two ways in which recorders can be coupled to digital system.

## OR

10 a. Draw the circuit diagram of 3-bit R-2R Ladder DAC and write the expression for output voltage for a digital input data of 100 and 001 .
(04 Marks)
b. With the help of functional diagram explain the working principle of successive approximation ADC
(07 Marks)
c. A dual slope ADC uses a 16 -bit counter and a 4 MHz clock rate. The maximum input voltage is +10 V . the maximum integrator output voltage should be -8 V . When the counter has cycled through $2^{2}$ counts. The capacitor used in the integrator is $0.1 \mu \mathrm{~F}$. Findthe of the ${ }_{-}$ resistor R of the integrator.
(05 Marks)


15EI/BM/ML43

# Fourth Semester B.E. Degree Examination, June/July 2017 <br> Embedded Controllers 

Time: 3 hrs .

Max. Marks: 80

Note: Answer FIVE full questions, choosing one full question from each module.

## Module-1

1 a. List the architectural difference between:
i) Harvard and Von Neumann architecture
ii) RISC and CISC architecture
(08 Marks)
b. Compare 8051,8052 and 8031 microcontrollers.
(04 Marks)
c. Discuss briefly the developments in microprocessor technology.

## OR

2 a. Explain the neat block diagram, the architecture of 8051 microcontroller. ( $\mathbf{2 8}$ Marks)
b. Explain the following pins and their functions in 8051 microcontroller:
i) ALE
ii) $\overline{\text { PSEN }}$
iii) $\overline{\mathrm{EA}}$
iv) $\overline{\mathrm{RD}}$
v) $R X \bar{D}$
(05 Marks)
c. Sketch and explain the internal RAM organization of 8051 microcontroller.
(03 Marks)

## Module-2

3 a. List and explain with examples, different addressing modes of 8051 microcontrollers.
(06 Marks)
b. Illustrate with examples, the instructions related to stack operations.
(04 Marks)
c. Identify the type of addressing modes used in the following instructions:
i) $\mathrm{ADD} \mathrm{A}, 30 \mathrm{~h}$
ii) CJNE A, \#29h, again
iii) 1NC@R1
iv) $\mathrm{XCH} \mathrm{A}, \mathrm{R} 3$
v) CLR C
vi) AJMP label
(04 Marks)

## OR

4 a. Differentiate between jump and call instructions of 8051 microcontroller. Explain with suitable example, different range of jump and call instructions.
(06 Marks)
b. Evaluate the following instructions and identify the contents of A in each step:

```
MOV A, #OASH
RR A
RR A
SWAP A
CLR C
RRC A
RL A
SWAP A
```

(04 Marks)
c. Write an ALP in 8051 to count the number of 1 's and 0 's in a number stored in memory location 30 h .
(06 Marks)

## Module-3

5 a. Explain different data types in 8051 C.
(04 Marks)
b. Write a C program in 8051 to toggle all bits of P0 and P2 continuously with 250 ms delay. Use inverting operator.
(04 Marks)
c. Show an interface of 8051 microcontroller with a stepper motor drive circuit and explain its principle of operation.
(08 Marks)

## OR

6 a. Interface an LCD display unit to 8051 microcontroller and write an ALP to display the message "HELLO".
(10 Marks)
b. With a neat block diagram, illustrate the interfacing of 8051 microcontroller to DAC 0808 at port P1 and write a 8051 program to generate triangular waveform.
(06 Marks)

## Module-4

7 a. Discuss the different modes of timers in 8051 microcontroller with neat block diagram.
(06 Marks)
b. Explain how 8051 transmits the character and receives a character serially using its UART.
(06 Marks)
c. Explain briefly, the interrupts of 8051. Indicate their vector addresses.
(04 Marks)

## OR

8 a. Write a C program for 8051 to generate a square wave of frequency 10 kHz on pin P1.4. Use timer 0 in mode 2 with XTAL $=22 \mathrm{MHz}$.
(06 Marks)
b. Explain SCON register with its bit pattern.
(04 Marks)
c. Explain IE and IP registers with their bit pattern and show how priorities change with example.
(06 Marks)

## Module-5

9 a. Explain with neat diagram, the typical architectures of MSP430 microcontroller.
(12 Marks)
b. Explain briefly the low power applications of MSP430 microcontroller.
(04 Marks)
OR
10 a. Discuss the clock system of MSP430 microcontroller.
(06 Marks)
b. Give details of memory map of MSP430 microcontroller.
(06 Marks)
c. Mention different addressing modes of MSP430 microcontrollers.
(04 Marks)

## CBCS SCAEME

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15ML45

## Fourth Semester B.E. Degree Examination, June/July 2017 <br> Biomedical Instrumentation

Time: 3 hrs.
Max. Marks: 80
Note: Answer FIVE full questions, choosing one full question from each module.

## Module-1

1 a. Discuss the components of Man - Instrument system.
(08 Marks)
b. Explain the following with necessary diagram and graph :
i) Resting potential
ii) Action potential.
(08 Marks)

2 a. Define Bioelectric potentials and explain its types.
(08 Marks)
b. Discuss the problems encountered in measuring a living system.
(08 Marks)

## Module-2

3 a. Explain Half cell potential. (06 Marks)
b. Summarize the importance of Electrode Impedance.
(04 Marks)
c. List out the effects of Skin Abrasion.
(06 Marks)
OR
4 a. Analyse Electrode - Electrolyte Interface with necessary diagram. (08 Marks)
b. Illustrate the following: i) Capacitive Electrodes ii) Stimulative Electrodes. ( 08 Marks)

## Module-3

5 a. With a block diagram, explain Pulse Rate Measurement. (08 Marks)
b. Explain Auscultatory method used for measuring Blood Pressure. (08 Marks)

## OR

6 a. Analyse the instruments used for testing motor responses. (08 Marks)
b. Discuss about Bio feedback Instrumentation.
(08 Marks)

## Module-4

7 a. Explain Common mode and other Interference Reduction circuits.
(06 Marks)
b. Discuss the working of AC carrier amplifier with relevant circuit diagram.
(10 Marks)

## OR

8 a. Summarize the problems frequently encountered with bioamplifiers. (09 Marks)
b. Illustrate Transient Protection.
(07 Marks)

## Module-5

9 a. With necessary circuit, explain the following: i) integrators ii) Comparators. (08 Marks)
b. Discuss the Amplifiers used for measuring Biopotential signals.
(08 Marks)

## OR

10 a. Differentiate between Modulators and Demodulators.
(04 Marks)
b. Discuss Biopotential Preamplifier, with an example and a relevant circuit.


Fourth Semester B.E. Degree Examination, June/July 2017

## Scientific and Analytical Instrumentation

Time: 3 hrs .

Note: Answer FIVE full questions, choosing one full question from each module.

## Module-1

1 a. Explain the major steps in solving an analytical problem.
(08 Marks)
b. Define spectroscopy. Explain the energy-level diagram for a diatomic molecule.
(08 Marks)

## OR

2 a. What are the principal types of chemical instrumentation?
(04 Marks)
b. Explain the nature of electromagnetic radiation.
(08 Marks)
c. Write a note on vibration energy levels.
(04 Marks)

3 a. Write notes on:
i) Dispersion,
ii) Resolution.
(04 Marks)
b. Explain gratings used as dispersive devices.
(08 Marks)
c. Explain with schematic interference filter.
(04 Marks)

4 a. Discuss about the mirror and lenses used in ultraviolet and visible spectrometry instrumentation.
(06 Marks)
b. Explain the three different Littrow mounting configuration for wavelength selection.
(10 Marks)

## Module-3

5 a. Explain the schematic diagram of equipment for atomic fluorescence spectrometry (AFS).
b. Discuss about the role of combustion flames in FES and AAS.
c. Write a note on Nebulization.

## OR

6 a. Explain flame atomization processes for the salt MX.
(07 Marks)
b. Write the applications of FES and AAS.
(03 Marks)
c. Explain about atomic absorption measurements and results with a necessary figure.
(06 Marks)

## Module-4

7 a. Define chromatography. Explain the block diagram of a gas chromatograph.
(07 Marks)
b. Explain the circuit arrangement for measuring the changes in the resistance produced in the Katharometer cell elements.
c. Explain the thin layer amperometric detector.

## OR

8 a. Discuss about the separation columns in HPL instrumentation.
(07 Marks)
b. Explain the single type pump used in HPLC.
(05 Marks)
c. Write the circuit diagram for measurement of area under the chromatographic peak.
(04 Marks)

## Module-5

9 a. What is a blood gas analyzer?
(02 Marks)
b. Write the circuit diagram for computation of:
i) Bicarbonate $\left(\mathrm{HCO}_{3}\right)$
ii) Total $\mathrm{CO}_{2}$
iii) Base excell.
c. Explain the measurement of Ozone in air using the oxidizing properties of Ozone. ( $\mathbf{0 8}$ Marks)

## OR

10 a. Explain the catheter tip electrode for measurement of $\mathrm{pO}_{2}$ and $\mathrm{pCO}_{2}$.
(08 Marks)
b. Explain the flow diagram for the measurement of total oxidants in air.
(08 Marks)

## CBCS Scheme

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15MATDIP41

Fourth Semester B.E. Degree Examination, June/July 2017
Additional Mathematics - II

Time: 3 hrs.
Max. Marks: 80

## Note: Answer any FIVE full questions, choosing ONE full question from each module.

## Module-1

1 a. Find the rank of the matrix :
$\left[\begin{array}{llll}1 & 2 & 3 & 2 \\ 2 & 3 & 5 & 1 \\ 1 & 3 & 4 & 5\end{array}\right]$ by elementary row transformations.
b. Solve the following system of equations by Gauss elimination method :

$$
\begin{aligned}
& 2 x+y+4 z=12 \\
& 4 x+11 y-z=33 \\
& 8 x-3 y+2 z=20
\end{aligned}
$$

(05 Marks)
c. Find all the eigen values and eigen vector corresponding to largest eigen value of the matrix:
$\left[\begin{array}{lll}1 & 1 & 3 \\ 1 & 5 & 1 \\ 3 & 1 & 1\end{array}\right]$.

## OR

2 a. Solve the following system of equations by Gauss elimination method:
$x+y+z=9$
$2 x+y-z=0$
$2 x+5 y+7 z=52$.
(06 Marks)
b. Reduce the matrix $\left[\begin{array}{lll}1 & 2 & 3 \\ 1 & 4 & 2 \\ 2 & 6 & 5\end{array}\right]$ into its echelon form and hence find its rank. (05 Marks)
c. Find the inverse of the matrix $\mathrm{A}=\left[\begin{array}{ll}1 & 4 \\ 2 & 3\end{array}\right]$ using Cayley - Hamilton theorem. (05 Marks)

## Module-2

3 a. Solve $\left(D^{2}-4 D+13\right) y=\cos 2 x$ by the method of undetermined coefficients. ( 06 Marks)
b. Solve $\left(D^{2}+2 D+1\right) y=x^{2}+2 x$.
(05 Marks)
c. Solve $\left(D^{2}-6 D+25\right) y=\sin x$.
(05 Marks)

4 a. Solve $\left(D^{2}+1\right) y=\tan x$ by the method of variation of parameters.
(06 Marks)
b. Solve $\left(D^{3}+8\right) y=x^{4}+2 x+1$.
(05 Marks)
c. Solve $\left(D^{2}+2 D+5\right) y=e^{-x} \cos 2 x$.
(05 Marks)

## Module-3

5 a. Find the Laplace transforms of :
i) $e^{-t} \cos ^{2} 3 t$
ii) $\frac{\cos 2 t-\cos 3 t}{t}$.
(06 Marks)
b. Find:
i) $L\left[t^{-5 / 2}+t^{5 / 2}\right]$
ii) $L[\sin 5 t \cdot \cos 2 t]$.
(05 Marks)
c. Find the Laplace transform of the function: $f(t)=E \sin \left(\frac{\pi t}{\omega}\right), 0<t<\omega$, given that $\mathrm{f}(\mathrm{t}+\omega)=\mathrm{f}(\mathrm{t})$.
(05 Marks)

## OR

6 a. Find :
i) $L\left\lfloor t^{2} \sin t\right\rfloor$
ii) $\mathrm{L}\left[\frac{\sin 2 \mathrm{t}}{\mathrm{t}}\right]$.
(06 Marks)
b. Evaluate : $\int_{0}^{\infty} \frac{\cos 6 \mathrm{t}-\cos 4 \mathrm{t}}{\mathrm{t}} \mathrm{dt}$ using Laplace transform.
(05 Marks)
c. Express $f(t)=\left\{\begin{array}{cc}\sin 2 t, & 0<t<\pi \\ 0, & t>\pi\end{array}\right.$, in terms of unit step function and hence find $L[f(t)]$.
(05 Marks)

## Module-4

7 a. Solve the initial value problem $\frac{d^{2} y}{d x^{2}}+\frac{5 d y}{d x}+6 y=5 e^{2 x}, y(0)=2, y^{\prime}(0)=1$ using Laplace transforms.
(06 Marks)
b. Find the inverse Laplace transforms: i) $\frac{3\left(s^{2}-1\right)^{2}}{2 s^{2}} \quad$ ii) $\frac{s+1}{s^{2}+6 s+9}$.
(05 Marks)
c. Find the inverse Laplace transform : $\log \left[\frac{s^{2}+4}{s(s+4)(s-4)}\right]$.
(05 Marks)

OR
8 a. Solve the initial value problem :
$\frac{d^{2} y}{d t^{2}}+\frac{4 d y}{d t}+3 y=e^{-t}$ with $y(0)=1=y^{\prime}(0)$ using Laplace transforms.
(06 Marks)
b. Find the inverse Laplace transform :

$$
\text { i) } \frac{1}{s \sqrt{5}}+\frac{3}{s^{2} \sqrt{5}}-\frac{8}{\sqrt{5}} \quad \text { ii) } \frac{3 s+1}{(s-1)\left(s^{2}+1\right)} \text {. }
$$

(05 Marks)
c. Find the inverse Laplace transform : $\frac{2 s-1}{s^{2}+4 s+29}$.
(05 Marks)

## Module-5

9 a. State and prove Baye's theorem.
(06 Marks)
b. A can hit a target 3 times in 5 shots, B 2 times in 5 shots and C 3 times in 4 shots. They fire a volley. What is the probability that i) two shots hit ii) atleast two shots hit?
(05 Marks)
c. Find $P(A), P(B)$ and $P(A \cap \bar{B})$, if $A$ and $B$ are events with $P(A \cup B)=\frac{7}{8}$, $\mathrm{P}(\mathrm{A} \cap \mathrm{B})=\frac{1}{4}$ and $\mathrm{P}(\overline{\mathrm{A}})=\frac{5}{8}$.
(05 Marks)

## OR

10 a. Prove that $P(A \cup B)=P(A)+(B)-P(A \cap B)$, for any two events $A$ and $B$.
(06 Marks)
b. Show that the events $\bar{A}$ and $\bar{B}$ are independent, if $A$ and $B$ are independent events.
(05 Marks)
c. Three machines A, B and C produce respectively $60 \%, 30 \%, 10 \%$ of the total number of items of a factory. The percentage of defective output of these machines are respectively $2 \%, 3 \%$ and $4 \%$. An item is selected at random and is found defective. Find the probability that the item was produced by machine C .
(05 Marks)

